Multivariate Change Detection on High Resolution Monovariate SAR Image Using Linear Time-Frequency Analysis

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Motivations

Change detection between two $\begin{bmatrix} \mathbf{I} = [\mathbf{i}_1, \mathbf{i}_2, \dots, \mathbf{i}_K] \in \mathbb{C}^{p \times K} \\ \mathbf{J} = [\mathbf{j}_1, \mathbf{j}_2, \dots, \mathbf{j}_K] \in \mathbb{C}^{p \times K}$ multivariate images I and J:

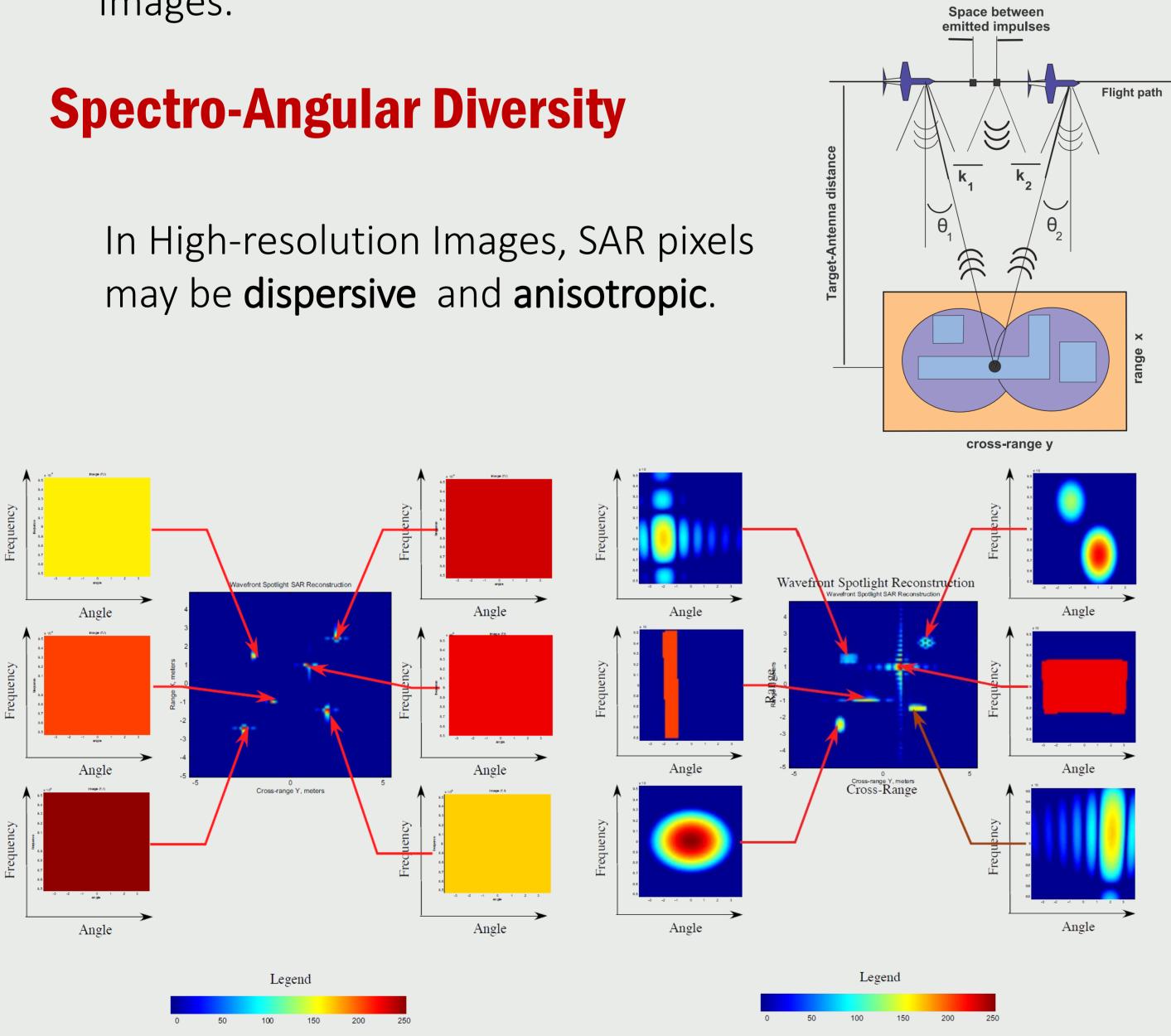
$$\forall k, \mathbf{i}_k \sim \mathcal{CN}(\mathbf{0}_p, \mathbf{C}_i) \text{ and } \mathbf{j}_k \sim \mathcal{CN}(\mathbf{0}_p, \mathbf{C}_j)$$

 $H_0 : \mathbf{C}_i = \mathbf{C}_j$ $H_1 : \mathbf{C}_i \neq \mathbf{C}_j$ **Detection Problem:**

Detector:
$$\hat{\Lambda}_{\text{GLRT}} = \frac{\left|\frac{1}{2K}\left(\sum_{k=1}^{K}\mathbf{i}_{k}\,\mathbf{i}_{k}^{H} + \sum_{k=1}^{K}\mathbf{j}_{k}\,\mathbf{j}_{k}^{H}\right)\right|^{2K}}{\left|\frac{1}{K}\sum_{k=1}^{K}\mathbf{i}_{k}\,\mathbf{i}_{k}^{H}\right|^{K}\left|\frac{1}{K}\sum_{k=1}^{K}\mathbf{j}_{k}\,\mathbf{j}_{k}^{H}\right)\right|^{K}}.$$

Polarimetric (p=3) diversity is generally used but not available for monovariate images.

Idea: Use Spectro-Angular Diversity in High-Resolution SAR Images.



Isotropic and white scatterers

anisotropic and colored scatterers



Construction Of Diversity

Traditional SAR reconstruction:

$$I(\mathbf{r}) = \int_{\mathcal{D}} H(\mathbf{k}) \exp\left(2\,i\,\pi\,\mathbf{k}^T\,\mathbf{r}\right)$$

With: **r**, pixel position $\mathbf{k} = [k\cos(\theta), k\sin(\theta)]^T$, wave vector *H*, backscattering coefficient \mathcal{D} , frequency and angular support of H

Use of short time Fourier Transform:

 $W_{l,m}(\mathbf{r}) = \int_0^{2\pi} \mathrm{d}\theta \int_0^{+\infty} k \ H(k,\theta) \ \phi_{l,m}(k,\theta) \ e^{+j2\pi\mathbf{k}^T\mathbf{r}} \ \mathrm{d}k$ With: $\phi_{l,m}(k,\theta) = \begin{cases} 1 \text{ if } (k,\theta) \in \Delta_{l,m} \\ 0 \text{ otherwhise} \end{cases}$

$$\mathcal{D} = [k_{\min}, k_{\max}] \cup [\theta_{\min}, \kappa_{\max}] \cup [\theta_{\min}, \kappa_{\max}]$$

$$\kappa = k_{\max} - k_{\min}, \Theta = \theta_{\max}$$

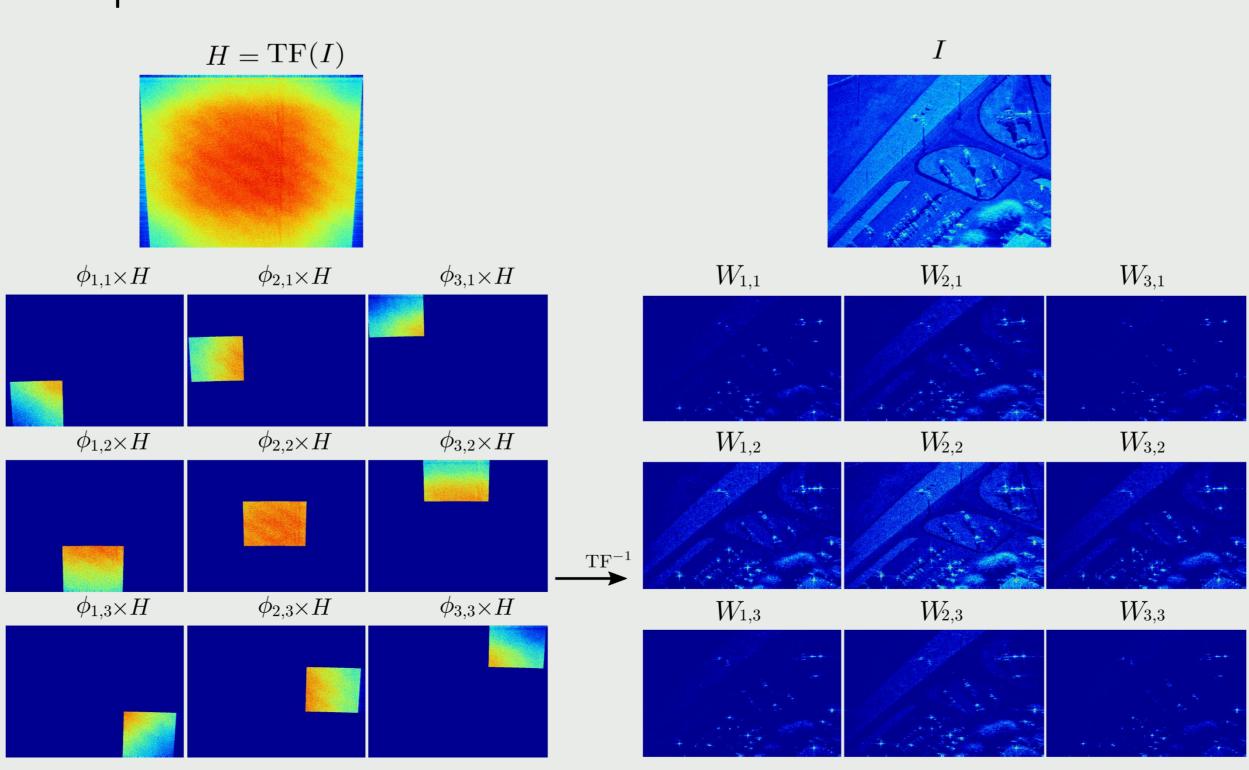
$$\Delta_{l,m} = \left[k_{\min} + \frac{(l-1)\kappa}{N_k}, \kappa_{\max}\right]$$

$$\cup \left[\theta_{\min} + \frac{(m-1)\kappa}{N_{\theta}}\right]$$

For each pixel, we obtain a vector:

$$\mathbf{i} = [W_{1,1}(x,y), W_{1,2}(x,y)]$$

Example with 3 Sub-Bands and 3 Sub-Looks:



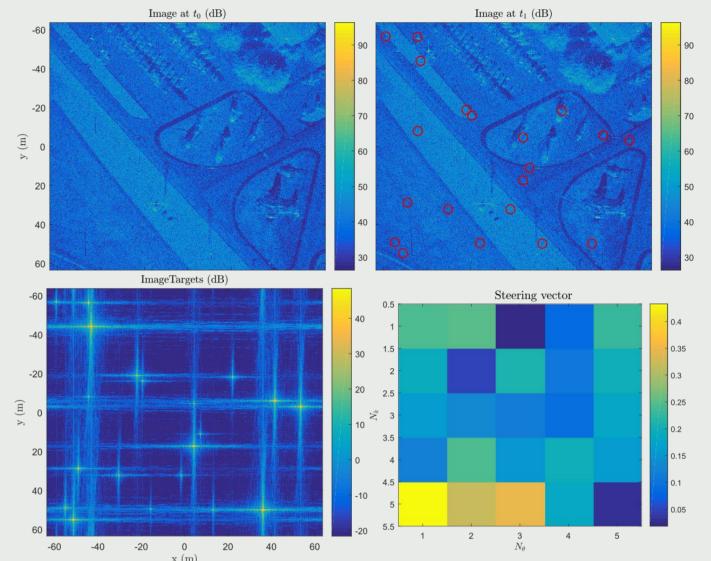
$d\mathbf{k}$

 $[\theta_{max}]$ $-\theta_{min}$ $\overline{N_k}$ $\frac{1}{2}\Theta$, $\theta_{\min} + \frac{m\Theta}{N_{\theta}}$

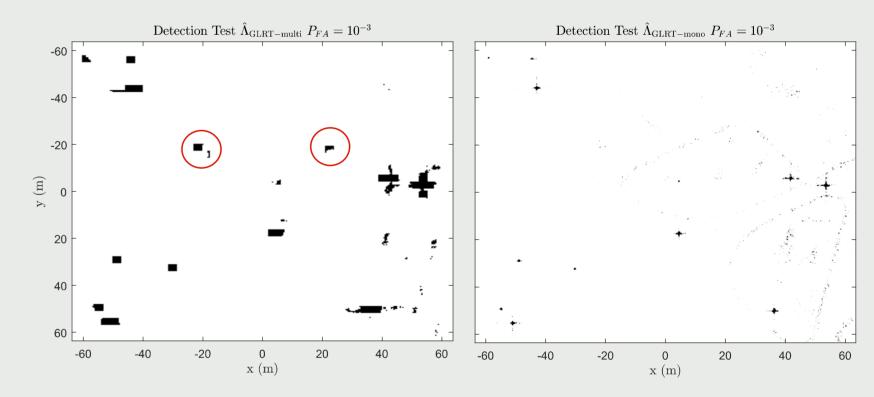
- $(Y), \ldots, W_{N_k, N_\theta}(x, y)]^T$

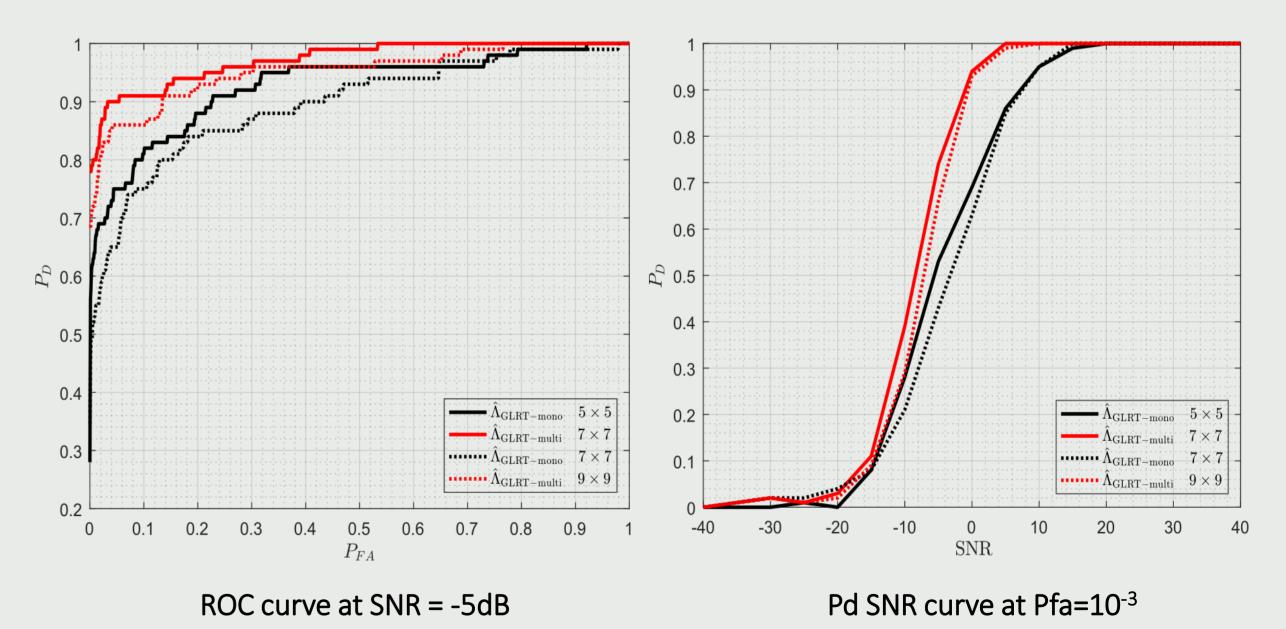
Simulations and Results

Dataset: SANDIA National Labs High Resolution SAR Image with artificially embedded targets.



Test of detection at Pfa=10⁻³ with spectro-angular diversity (p=25, left) and without (p=1, right):





Conclusion

A new methodology for Change Detection using Spectro-Angular Diversity has been proposed. The performances were evaluated and prove to be better when using this diversity rather than working on the amplitude alone.

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Performances estimation with Monte-Carlo Trials: